

# CHAPTER 5

# Parallel and Intersecting Lines

VEDA  
ACADEMY

CLASS 7<sup>TH</sup>

## NCERT EXERCISE AND SOLUTIONS - MATHEMATICS

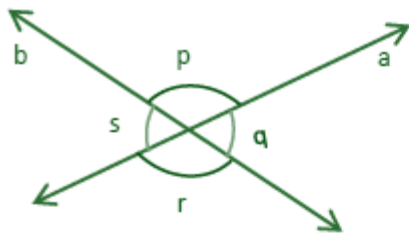
1. Can two straight lines intersect at more than one point? Solution:

### SOLUTION:

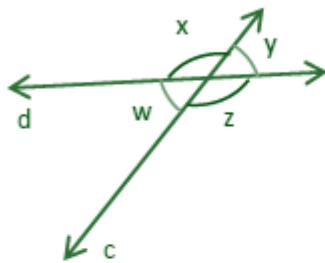
No, two straight lines cannot intersect at more than one point. If two lines intersect at more than one point, then they are coincident lines.

**Activity 1:** Draw two lines on a plain sheet of paper so that they intersect. Measure the four angles formed with a protractor. Draw four such pairs of intersecting lines and measure the angles formed at the points of intersection.

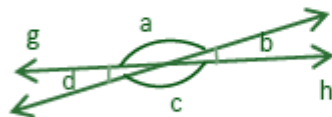
### SOLUTION:



$$\begin{aligned}\angle p \text{ and } \angle r &= 130^\circ \\ \angle q \text{ and } \angle s &= 50^\circ\end{aligned}$$

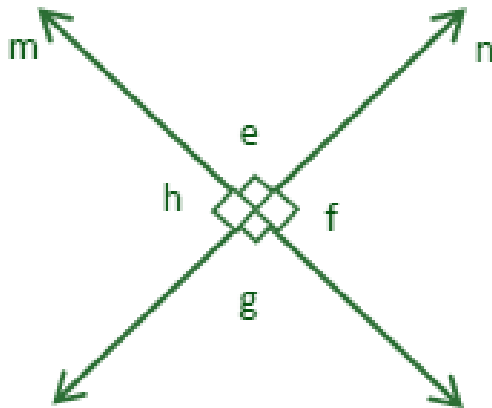


$$\begin{aligned}\angle x \text{ and } \angle z &= 150^\circ \\ \angle w \text{ and } \angle y &= 30^\circ\end{aligned}$$



$$\begin{aligned}\angle a \text{ and } \angle c &= 165^\circ \\ \angle p \text{ and } \angle n &= 15^\circ\end{aligned}$$





$\angle e$  and  $\angle g = 90^\circ$   
 $\angle h$  and  $\angle f = 90^\circ$

3. What patterns do you observe among these angles?

**SOLUTION:**

It is observed that the sum of adjacent angles formed by the intersection of two lines is  $180^\circ$ , and the vertically opposite angles are equal in measure.

4. Is this always true for any pair of intersecting lines?

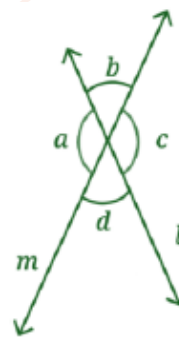
**SOLUTION:**

Yes, any pair of intersecting lines form vertically opposite angles, which are equal in measure.

**FIGURE IT OUT**

1. List all the linear pairs and vertically opposite angles you observe in Fig. 5.3:

Linear Pairs	$\angle a$ and $\angle b$ , ...
Pairs of Vertically Opposite Angles	$\angle b$ and $\angle d$ ...



Ans:

Linear pair angles:  $\angle a$  and  $\angle b$ ;  $\angle b$  and  $\angle c$ ;  $\angle c$  and  $\angle d$ ;  $\angle a$  and  $\angle d$ .

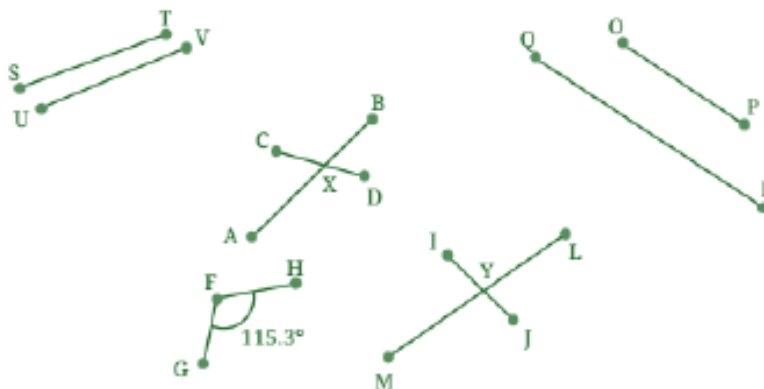
Vertically opposite angles:  $\angle a$  and  $\angle c$ ;  $\angle b$  and  $\angle d$ .

5. Observe Figure and describe the way the line segments meet or cross each other in each case, with appropriate mathematical words (a point, an endpoint, the midpoint, meet, intersect) and the degree measure of each angle.

For example, line segments FG and FH meet at the endpoint F at an angle of  $115.3^\circ$ .

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Are line segments ST and UV likely to meet if they are extended?  
 Are line segments OP and QR likely to meet if they are extended?

**SOLUTION:**

No, the line segments ST and UV, as well as OP and QR, will not meet if extended, as they are parallel lines that never intersect.

6. Which pairs of lines appear to be parallel in Fig. 5.6 below?

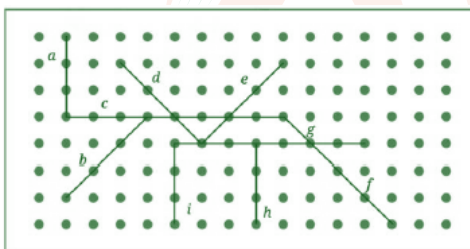


Fig. 5.6

**SOLUTION:**

Lines a, i and h are parallel to each other.  
 Line b is parallel to line e.  
 Line c is parallel to line g.  
 Line d is parallel to line f.

Activity 2: Take a plain square sheet of paper (use a newspaper for this activity).

- How would you describe the opposite edges of the sheet? They are \_\_\_\_\_ to each other.

**SOLUTION:**

They are parallel to each other.

- How would you describe the adjacent edges of the sheet? The adjacent edges are \_\_\_\_\_ to each other. They meet at a point. They form right angles.

**SOLUTION:**

The adjacent edges are perpendicular to each other.



- Fold the sheet horizontally in half. A new line is formed (see Fig. 5.7).
- How many parallel lines do you see now? How does the new line segment relate to the vertical sides?

**SOLUTION:**

We see three parallel horizontal lines — the top edge, the fold, and the bottom edge. The new horizontal line is perpendicular to the vertical sides.

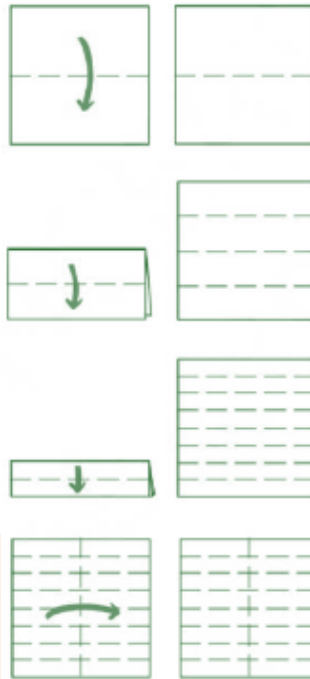


Fig. 5.7

- Make one more horizontal fold in the folded sheet. How many parallel lines do you see now?

**SOLUTION:**

Now, we see five parallel horizontal lines.

- What will happen if you do it once more? How many parallel lines will you get? Is there a pattern? Check if the pattern extends further, if you make another horizontal fold.

**SOLUTION:**

We will get nine parallel lines. The pattern follows:

- 1st fold → 3 lines
- 2nd fold → 5 lines
- 3rd fold → 9 lines

So, after each fold, the number of horizontal lines approximately doubles and adds one. The pattern continues as you fold more.

- Make a vertical fold in the square sheet. This new vertical line is \_\_\_\_\_ to the previous horizontal lines.

**SOLUTION:**

The new vertical line is perpendicular to the previous horizontal lines.



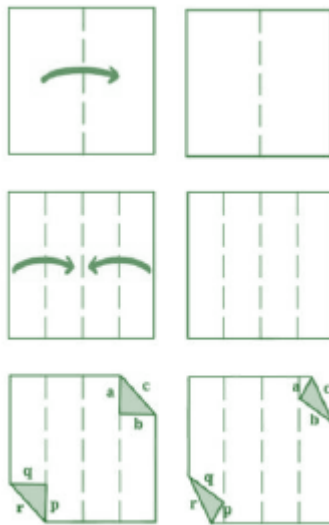
- Fold the sheet along a diagonal. Can you find a fold that creates a line parallel to the diagonal line?

**SOLUTION:**

Yes, we can make a fold parallel to the diagonal by folding the sheet in the same slanting direction at equal angles or by folding a smaller triangle inside the square.

Here is another activity for you to try.

- Take a square sheet of paper, fold it in the middle and unfold it.
- Fold the edges towards the centre line and unfold them.
- Fold the top right and bottom left corners onto the creased line to create triangles. Refer to Fig. 5.8.
- The triangles should not cross the crease lines.
- Are a, b and c parallel to p, q and r respectively? Why or why not?



**SOLUTION:**

Yes, a, b, and c are parallel to p, q, and r, respectively.

a (top edge) is parallel to p (bottom edge).

b (right edge) is parallel to q (left edge).

c and r are diagonal folds made symmetrically, so they are parallel.

**FIGURE IT OUT**

1. Draw some lines perpendicular to the lines given on the dot paper in Fig. 5.10.



Fig. 5.10

**Ans:**

Do it yourself

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2. In Fig. 5.11, mark the parallel lines using the notation given above (single arrow, double arrow etc.). Mark the angle between perpendicular lines with a square symbol.

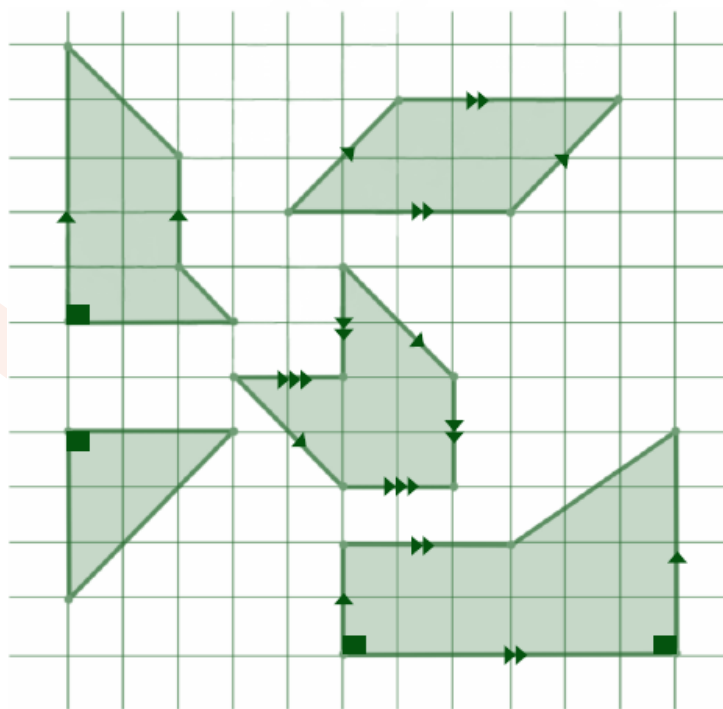
(a) How did you spot the perpendicular lines?

(b) How did you spot the parallel lines?



Fig. 5.11

Ans:



(i) Lines that intersect at a  $90^\circ$  angle are called perpendicular lines.

(ii) Lines that do not meet, no matter how far they are extended, are called parallel lines.

3. In the dot paper following, draw different sets of parallel lines. The line segments can be of different lengths but should have dots as endpoints.

Ans:

Do it yourself



4. Using your sense of how parallel lines look, try to draw lines parallel to the line segments on this dot paper.

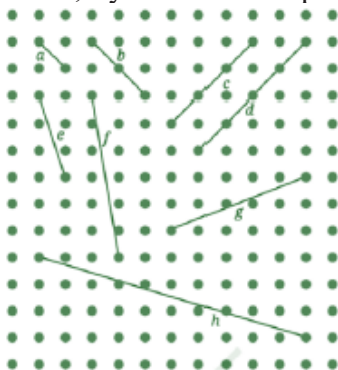


Fig. 5.12

- (a) Did you find it challenging to draw some of them?  
 (b) Which ones?  
 (c) How did you do it?

Ans:

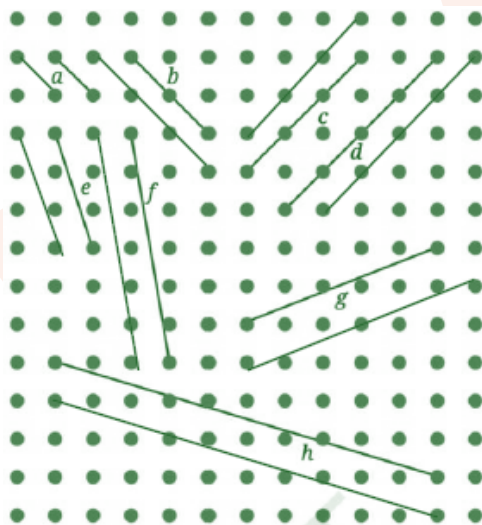


Fig. 5.12

- (a) Yes, some line segments are a little more difficult to draw than others.  
 (b) Line segments e, f, h, and g.  
 (c) Parallel lines are drawn by keeping them equidistant from the given line throughout their length.
5. In Fig. 5.13, which line is parallel to line a — line b or line c? How do you decide this?

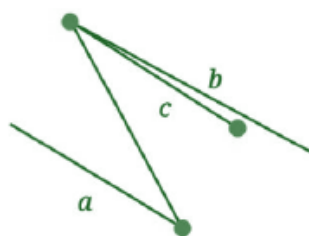


Fig. 5.13

Ans:

Line a is parallel to line c because both lines remain equidistant from each other and do not intersect, no matter how far they are extended.



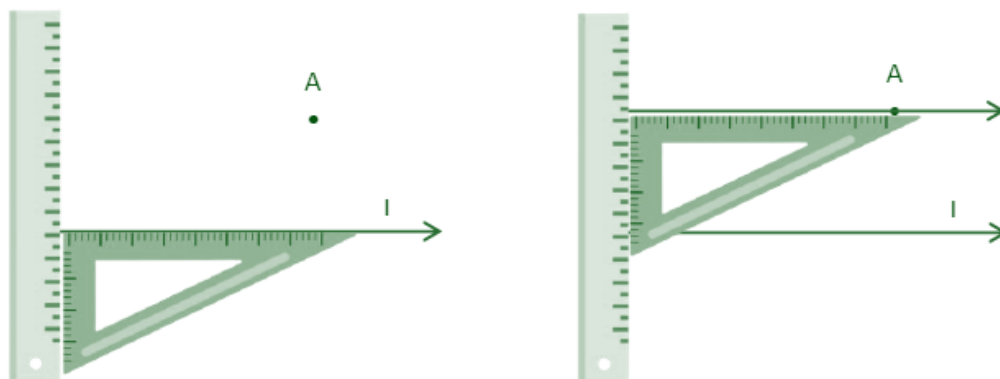
7. Can you draw a line parallel to  $l$ , that goes through point  $A$ ? How will you do it with the tools from your geometry box? Describe your method.



Fig. 5.23

**SOLUTION:**

Yes, we can draw a line parallel to  $l$  that goes through point  $A$  using set squares, ruler and pencil.

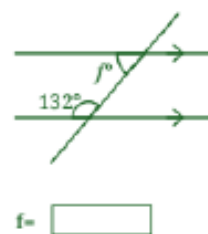
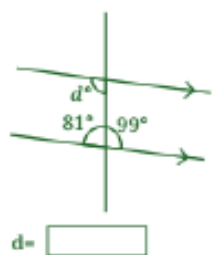
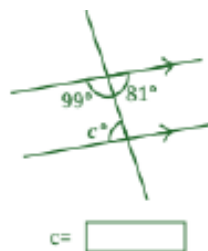
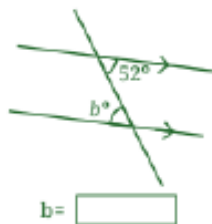
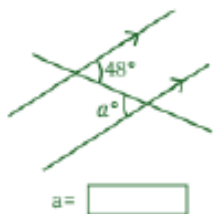


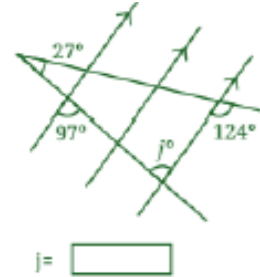
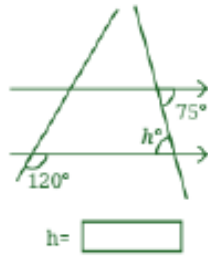
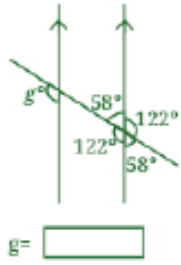
Steps of construction:

- (i) Align one edge of the set square with line  $l$ .
- (ii) Place a ruler along the other perpendicular edge.
- (iii) Slide the set square along the ruler until it reaches point  $A$ .
- (iv) Draw a line through  $A$  along the set square's edge.
- (v) This is the required line parallel to  $l$ .

**FIGURE IT OUT**

1. Find the angles marked below.

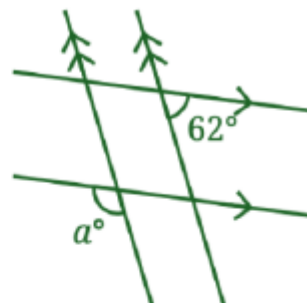
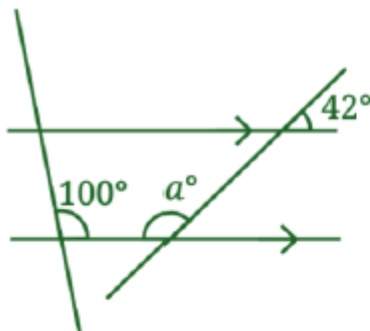




Ans:

- Since alternate interior angles formed by a transversal intersecting a pair of parallel lines are equal, angle a is  $48^\circ$ .
- Since alternate interior angles formed by a transversal intersecting a pair of parallel lines are equal, angle b is  $52^\circ$ .
- Since alternate interior angles formed by a transversal intersecting a pair of parallel lines are equal, angle c is  $81^\circ$ .
- Since alternate interior angles formed by a transversal intersecting a pair of parallel lines are equal, angle d is  $99^\circ$ .
- Since alternate interior angles formed by a transversal intersecting a pair of parallel lines are equal, angle e is  $69^\circ$ .
- Since the sum of interior angles on the same side of a transversal is always equal to  $180^\circ$ . Therefore,  $f + 132^\circ = 180^\circ$   
 $f = 180^\circ - 132^\circ$   
 $f = 48^\circ$ .
- Since corresponding angles formed by a transversal intersecting a pair of parallel sides are equal, angle g is  $122^\circ$ .
- Since alternate interior angles formed by a transversal intersecting a pair of parallel lines are equal, angle h is  $75^\circ$ .
- Since alternate interior angles formed by a transversal intersecting a pair of parallel lines are equal, angle i is  $54^\circ$ .
- Since alternate interior angles formed by a transversal intersecting a pair of parallel lines are equal, angle j is  $97^\circ$ .

2. Find the angle represented by a.



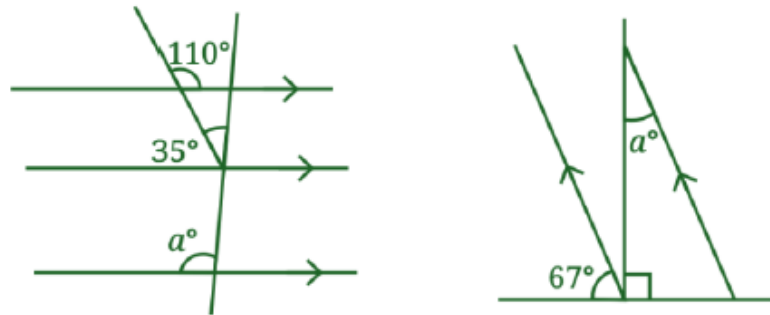
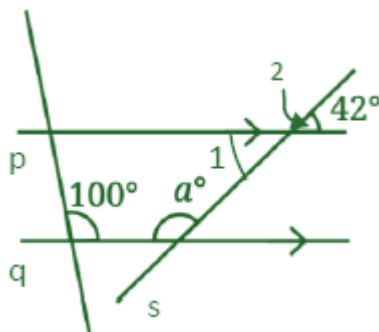


Fig. 5.31

Ans:

(A)



$\angle 1 = \angle 2 = 42^\circ$  .....(Vertically opposite angles)

Line p is parallel to q and s is a transversal, then

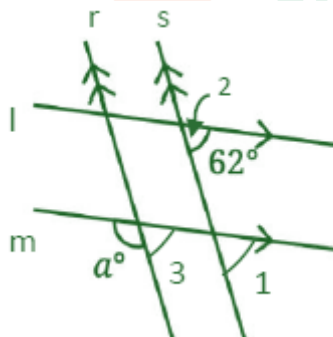
$a + \angle 1 = 180^\circ$  .....(Sum of interior angles on the same side of the transversal)

$$a + 42^\circ = 180^\circ$$

$$a = 180^\circ - 42^\circ$$

$$a = 138^\circ$$

(B)



Line l is parallel to line m and s is a transversal, then

$\angle 1 = \angle 2 = 62^\circ$  .....(Corresponding angles)

Line r is parallel to line s and m is a transversal, then

$\angle 1 = \angle 3 = 62^\circ$  .....(Corresponding angles)

$a + \angle 3 = 180^\circ$  .....(Linear pair angles)

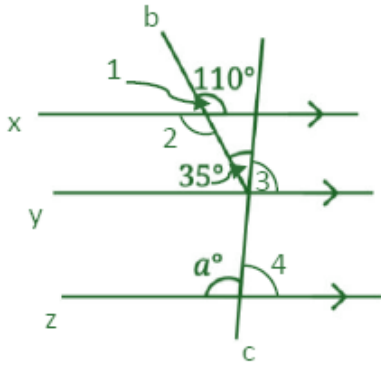
$$a + 62^\circ = 180^\circ$$

$$a = 180^\circ - 62^\circ$$

$$a = 118^\circ$$



(C)



$\angle 1 = \angle 2 = 110^\circ$  ..... (Vertically opposite angles)

Line x is parallel to line y and b is a transversal, then

$\angle 2 = 35^\circ + \angle 3$  ..... (Alternate interior angles)

or  $110^\circ = 35^\circ + \angle 3$

$110^\circ - 35^\circ = \angle 3$

or  $\angle 3 = 75^\circ$ .

Line y is parallel to line z and c is transversal, then

$\angle 3 = \angle 4 = 75^\circ$  ..... (Corresponding angles)

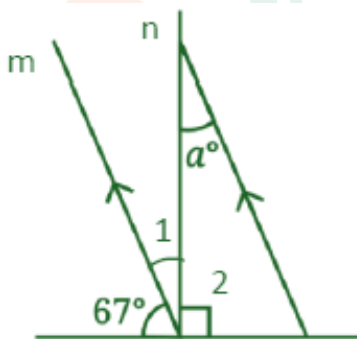
$a + \angle 4 = 180^\circ$  ..... (Linear pair angles)

$a + 75^\circ = 180^\circ$

$a = 180^\circ - 75^\circ$

$a = 105^\circ$ .

(D)



$\angle 1 + 67^\circ + \angle 2 = 180^\circ$  ..... (Sum of angles on a straight line)

$\angle 1 + 67^\circ + 90^\circ = 180^\circ$

$\angle 1 + 157^\circ = 180^\circ$

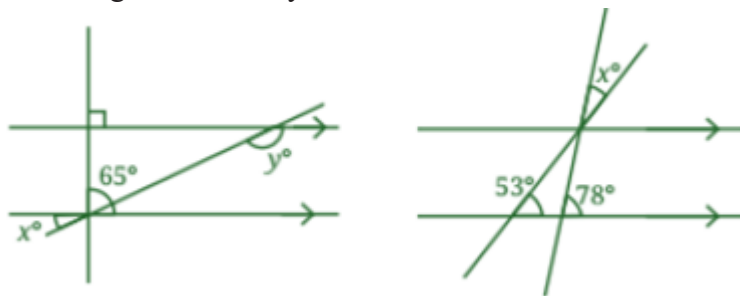
$\angle 1 = 180^\circ - 157^\circ$

$\angle 1 = 23^\circ$ .

$\angle 1 = \angle a = 23^\circ$  ..... (Alternate interior angles).

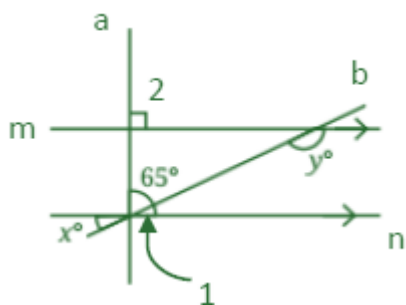


3. In the figures below, what angles do  $x$  and  $y$  stand for?



Ans:

(A)



Line  $l$  is parallel to line  $n$  and  $a$  is a transversal, then

$$\angle 2 = 65^\circ + \angle 1 \dots\dots\dots(\text{Corresponding angles})$$

$$90^\circ = 65^\circ + \angle 1$$

$$\angle 1 = 90^\circ - 65^\circ$$

$$\angle 1 = 25^\circ.$$

$$\angle 1 = x = 25^\circ \dots\dots\dots(\text{Vertically opposite angles})$$

Line  $m$  is parallel to line  $n$  and  $b$  is a transversal, then

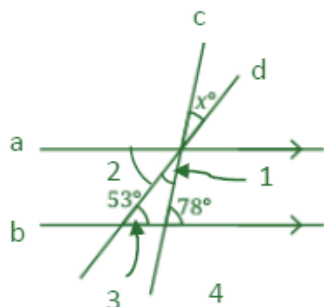
$$\angle 1 + \angle y = 180^\circ \dots\dots\dots(\text{Sum of interior angles on the same side of the transversal})$$

$$25^\circ + \angle y = 180^\circ$$

$$\angle y = 180^\circ - 25^\circ$$

$$\angle y = 155^\circ.$$

(B)



Line  $a$  is parallel to line  $b$  and  $d$  is a transversal, then

$$\angle 2 = \angle 3 = 53^\circ \dots\dots\dots(\text{Alternate interior angles})$$

Also, line  $a$  is parallel to line  $b$  and  $c$  is a transversal, then



$\angle 1 + \angle 2 = \angle 4$  ..... (Alternate interior angles)

or  $\angle 1 + 53^\circ = 78^\circ$

$\angle 1 = 78^\circ - 53^\circ$

$\angle 1 = 25^\circ$ .

Therefore,  $\angle 1 = x = 25^\circ$  .....(Vertically opposite angles).

4. In Fig. 5.33,  $\angle ABC = 45^\circ$  and  $\angle IKJ = 78^\circ$ . Find angles  $\angle GEH$ ,  $\angle HEF$ ,  $\angle FED$

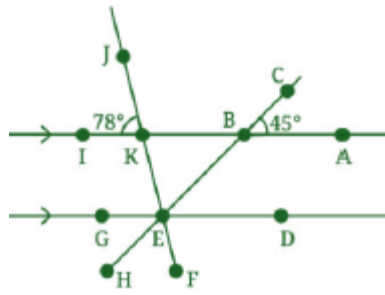


Fig. 5.33

Ans:

$\angle ABC = \angle KBE = 45^\circ$  .....(Vertically opposite angles)

$\angle IKJ = \angle BKE = 78^\circ$  .....(Vertically opposite angles)

$\angle BKE = \angle FED = 78^\circ$  .....(Corresponding angles)

$\angle KBE = \angle BED = 45^\circ$  .....(Alternate interior angles)

$\angle BED = \angle GEH = 45^\circ$  .....(Vertically opposite angles)

$\angle GEH + \angle HEF + \angle FED = 180^\circ$  .....(Sum of angles on a straight line)

$45^\circ + \angle HEF + 78^\circ = 180^\circ$

$123^\circ + \angle HEF = 180^\circ$

$\angle HEF = 180^\circ - 123^\circ$

$\angle HEF = 57^\circ$ .

5. In Fig. 5.34, AB is parallel to CD and CD is parallel to EF. Also, EA is perpendicular to AB. If  $\angle BEF = 55^\circ$ , find the values of x and y.

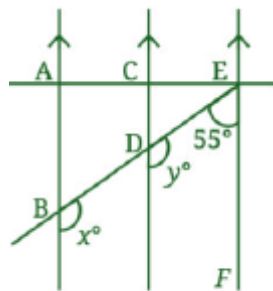


Fig. 5.34

Ans:

Since EF is parallel to CD and BE is a transversal, then



$\angle BEF + y = 180^\circ$  .....(Sum of interior angles on the same side of the transversal)

$55^\circ + y = 180^\circ$

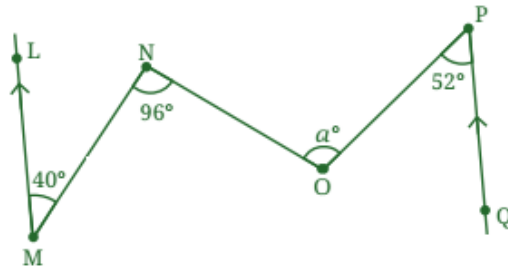
$y = 180^\circ - 55^\circ$

$y = 125^\circ$ .

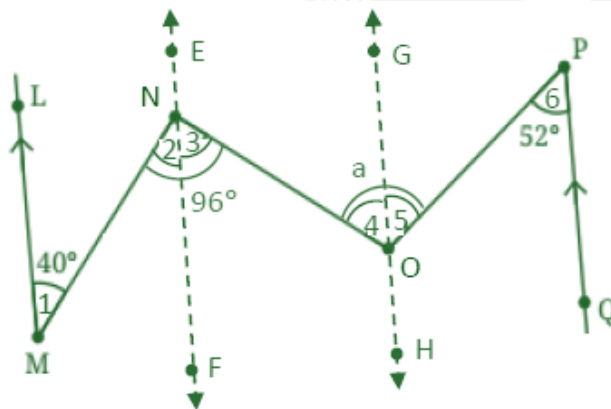
Since AB is parallel to CD and BE is a transversal, then

$x = y = 125^\circ$  ..... (Corresponding angles).

6. What is the measure of angle  $\angle NOP$  in Fig. 5.35?



Ans:



Construction: Draw lines EF and GH parallel to lines LM and PQ.

LM is parallel to EF and MN is a transversal, then

$\angle 1 = \angle 2 = 40^\circ$  ..... (Alternate interior angles)

$\angle 2 + \angle 3 = 96^\circ$

$40^\circ + \angle 3 = 96^\circ$

$\angle 3 = 96^\circ - 40^\circ$

$\angle 3 = 56^\circ$ .

EF is parallel to GH and NO is a transversal, then

$\angle 3 = \angle 4 = 56^\circ$  ..... (Alternate interior angles)

Also, GH is parallel to PQ and OP is a transversal, then

$\angle 5 = \angle 6 = 52^\circ$  ..... (Alternate interior angles)

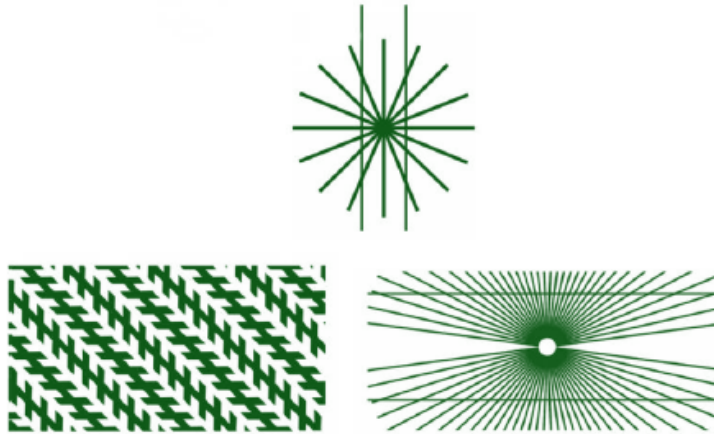
$a = \angle 4 + \angle 5$

$a = 56^\circ + 52^\circ$

$a = 108^\circ$ .



8. There do not seem to be any parallel lines here. Or, are there?



What causes these illusions?

**SOLUTION:**

Yes — there are parallel lines in all three images. The illusions are created by contextual visual cues (angles, perspective, and intersecting lines) that mislead your brain's interpretation of space and alignment.

